Hoare-style Specifications as Correctness Conditions for Non-Linearizable Concurrent Objects



Linearizable Concurrent Objects

Linearizability: A Correctness Condition for Concurrent Objects

MAURICE P. HERLIHY and JEANNETTE M. WING Carnegie Mellon University

A concurrent object is a data object shared by concurrent processes. Linearizability is a correctness condition for concurrent objects that exploits the semantics of abstract data types. It permits a high degree of concurrency, yet it permits programmers to specify and reason about concurrent objects using known techniques from the sequential domain. Linearizability provides the illusion that each operation applied by concurrent processes takes effect instantaneously at some point between its invocation and its response, implying that the meaning of a concurrent object's operations can be given by pre- and post-conditions. This paper defines linearizability, compares it to other correctness conditions, presents and demonstrates a method for proving the correctness of implementations, and shows how to reason about concurrent objects, given they are linearizable.

Non-overlapping calls to methods of a *concurrent* object should appear to take effect in their *sequential* order.

Linearizability is expensive

Laws of Order: Expensive Synchronization in Concurrent Algorithms Cannot be Eliminated

Hagit Attiya Technion hagit@cs.technion.il Rachid Guerraoui EPFL rachid.guerraoui@epfl.ch Danny Hendler Ben-Gurion University hendlerd@cs.bgu.ac.il

Petr Kuznetsov TU Berlin/Deutsche Telekom Labs pkuznets@acm.org Maged M. Michael IBM T. J. Watson Research Center magedm@us.ibm.com Martin Vechev IBM T. J. Watson Research Center mtvechev@us.ibm.com

Enabling better parallelism

The advent of multicore processors as the standard computing platform will force major changes in software design.

BY NIR SHAVIT

Data Structures in the Multicore Age

Relaxing the correctness condition would allow one to implement concurrent data structures more efficiently, as they would be free of synchronization bottlenecks.

Alternatives to linearizability

- Quiescent Consistency [Aspnes-al:JACM94]
- Quasi-Linearizability [Afek-al:OPODIS10]
- Quantitative Relaxation [Henzinger-al:POPL13]
- Quantitative Quiescent Consistency [Jagadeesan-Riely:ICALP14]
- Concurrency-Aware Linearizability [Hemed-Rinetzky:DISC15]
- Local Linearizability [Haas-al:CONCUR16]

Challenges of diversity

- Composing different conditions (CAL, QC, QQC) in a single program, which uses multiple objects;
- Providing *syntactic* proof methods for establishing all these conditions (akin to *linearization points*);
- Employing these criteria for *client-side reasoning* (*uniformity*).

Hoare-style Specifications as Correctness Conditions for Non-Linearizable Concurrent Objects



Hoare-style Specifications



If the initial state satisfies P, then, after **e** terminates, the final state satisfies Q (no matter the *interference* manifested by **C**).

Hoare-style Specifications

{ P } e { Q } @ C

- *Compositional* substitution principle;
- *Syntactic proof method* inference rules;
- Uniform reasoning about objects and their clients in the same proof system.

Hoare-style Specifications

{ P } e { Q } @ C

Rich • *Compositional* — substitution principle;

Live • *Syntactic proof method* — inference rules;

Two-sided • *Uniform* — reasoning about objects and their clients in the *same* proof system.

This work: Hoare-style specs as CAL, QC, QQC

Concurrency-Aware Linearizability (CAL):

Effects of some concurrent method calls should appear to happen simultaneously.

Quiescent Consistency (QC):

Method calls separated by a period of **no interference** (quiescence) should appear to take effect in their order.

This talk

Quantitative Quiescent Consistency (QQC):

The number of out-of-order method results is bounded by the number of interfering threads (with a constant factor).

Simple Counting Network

def getAndInc() : nat

Simple Counting Network



Simple Counting Network

```
def getAndInc() : nat = {
    b ← flip(bal);
    res ← fetchAndAdd2(x + b);
    return res;
}
```



```
def getAndInc() : nat = {
    b ← flip(bal);
    res ← fetchAndAdd2(x + b);
    return res;
}
```







 $T_{1}.b_{1} = 0$



Χ

2

x+1

1









 $T_{1}.b_{1} = 0$ $T_{1}.res_{1} = 0$ $T_{1}.b_{2} = 1$

def getAndInc() : nat = {
 b ← flip(bal);
 res ← fetchAndAdd2(x + b);
 return res;
}

bal 0



 $T_{1}.b_{1} = 0$ $T_{1}.res_{1} = 0$ $T_{1}.b_{2} = 1$ $T_{1}.res_{2} = 1$

```
def getAndInc() : nat = {
    b ← flip(bal);
    res ← fetchAndAdd2(x + b);
    return res;
}
```











 $T_{1}.b_{1} = 0$ $T_{2}.b_{1} = 1$











3



Correctness Conditions for Counting Network

No. calle to get And Inc () take effect in their sequential order

- **R**₁: different calls return *distinct* results (strong concurrent counter)
- R₂: two calls, separated by *period of quiescence*, take effect in their sequential order (QC)
- R₃: results of *two calls* in the same thread are out of order by no more than 2 * (number of calls *interfering with both*) (QQC)

Observations about the Counting Network

"Tokens"

- Every flip of the balancer grants thread a *capability* to add 2 to a counter (x or x+1);
- Each of the counters (x and x+1) changes continuously wrt. even/odd values

"Histories"

Real and Auxiliary State

- Hoare-style specs constrain state, auxiliary or real
- Real state heap (pointers bal, x, x+1);
- Auxiliary state any *fictional splittable* resource:
 - Token sets (τ) disjoint sets;
 - + Histories (χ) partial maps with **nat** as domain.

Auxiliary State of the Network



Interference-capturing histories



"timestamp", a value written to a counter \mathbf{x} or $\mathbf{x+1}$ (0, 1, 2, etc.)

Interference-capturing histories

 $X = \{ \dots, n \mapsto 0 \dots \}$ sets of tokens, held by interfering threads at the moment the entry has been written

Notation for Subjective Histories and Tokens

- **X**, **X** histories, contributed by **this** and *other* threads;
- **τ**, **τ** tokens, held by **this** and *other* threads

 $\{ \mathbf{T} = \emptyset \}$

res ← getAndInc() {∃ ι, $\mathbf{T}' = \emptyset$, $\mathbf{X}' = \mathbf{X} \cup (\operatorname{res} + 2) \mapsto \iota$, $\tau \subseteq \tau' \cup \operatorname{spent}(\chi' \setminus \chi)$, last($\mathbf{X} \cup \chi$) < res + 2 + 2 | ι∩ τ |}

 $\{ \mathbf{T} = \emptyset \} \leftarrow \text{no tokens held initially} \\ \text{by this thread} \\ \text{for each of the set of the set$

 $\{ \mathbf{T} = \emptyset \}$ Final tokens and self-history $\{ \exists \iota, \mathbf{T}' = \emptyset, \\ \mathbf{X}' = \mathbf{X} \cup (\operatorname{res} + 2) \mapsto \iota, \\ \tau \subseteq \tau' \cup \operatorname{spent}(\mathbf{X}' \setminus \mathbf{X}), \\ \operatorname{last}(\mathbf{X} \cup \mathbf{X}) < \operatorname{res} + 2 + 2 | \iota \cap \tau | \}$

 $\{ \mathbf{T} = \emptyset \}$

res \leftarrow getAndInc() { $\exists \iota, \mathbf{T}' = \emptyset,$ $\mathbf{X}' = \mathbf{X} \cup (\text{res} + 2) \mapsto \iota,$ $\tau \subseteq \tau' \cup \text{spent}(\chi' \setminus \chi),$ last($\mathbf{X} \cup \chi$) < res + 2 + 2 | $\iota \cap \tau$ |}

 $\{ \mathbf{T} = \emptyset \}$

 $res \leftarrow getAndInc() result + 2 is$ greater than any previous value in the history (modulo) $\mathbf{X}' = \mathbf{X} \cup (res + 2) \mapsto i, past \cap present interference)$ $\tau \subseteq \tau' \cup spent(\mathbf{X}' \setminus \mathbf{X}),$ $last(\mathbf{X} \cup \mathbf{X}) < res + 2 + 2 | i \cap \tau | \}$

What this spec is good for?

Implications of the spec for getAndInc

Each result corresponds to a fresh history entry

- R₁: different calls return *distinct* results (strong concurrent counter)
- R₂: two calls, separated by *period of quiescence*, take effect in their sequential order (QC)
- R₃: results of *two calls* in the same thread are out of order by no more than 2 * (number of calls *interfering with both*) (QQC)

Implications of the spec for getAndInc

- **R**₁: different calls return *distinct* results (strong concurrent counter)
- R₂: two calls, separated by *period of quiescence*, take effect in their sequential order (QC)
- R₃: results of *two calls* in the same thread are out of order by no more than 2 * (number of calls *interfering with both*) (QQC)

Exercising Quiescent Consistency

"quiescent moment"

- $(res_1, -) \leftarrow (getAndInc() || e_1);$
 - $(res_2, -) \leftarrow (getAndInc() | | e_2);$

return (res1, res2);

 $\{ ; res_1 < res_2 ? \}$

Specification of interfering program



Spec for parallel composition

$\{ \mathbf{T} = \emptyset \}$

(res₁, -) \leftarrow getAndInc() || e₁

$$\{ \exists \iota, \eta_1, \mathbf{T} = \emptyset, \\ \mathbf{X} = \mathbf{X} \cup \eta_1 \cup (\operatorname{res}_1 + 2) \mapsto \iota, \\ \tau \subseteq \tau' \cup \operatorname{spent}(\chi' \setminus \chi), \\ \operatorname{last}(\mathbf{X} \cup \chi) < \operatorname{res}_1 + 2 + 2 | \iota \cap \tau | \}$$

Spec for parallel composition

$\{ \mathbf{T} = \emptyset \}$

(res₁, -) \leftarrow getAndInc() || e₁

```
\{\exists \iota, \eta_1, \mathbf{T} = \emptyset, \\ \mathbf{X} = \mathbf{X} \cup \eta_1 \cup (\operatorname{res}_1 + 2) \mapsto \iota, \\ \tau \subseteq \tau' \cup \operatorname{spent}(\chi' \setminus \chi), \\ \operatorname{last}(\mathbf{X} \cup \chi) < \operatorname{res}_1 + 2 + 2 | \iota \cap \tau | \}
```

 $(res_1, -) \leftarrow getAndInc() || e_1;$ $(res_2, -) \leftarrow getAndInc() || e_2;$ return $(res_1, res_2);$ $(res_1, -) \leftarrow getAndInc() || e_1;$

$$(res_2, -) \leftarrow getAndInc() || e_2;$$

return
$$(res_1, res_2);$$

$$\{ \mathbf{T} = \emptyset \}$$

 $(\operatorname{res}_{1}, -) \leftarrow \operatorname{getAndInc}() || e_{1};$ $\{ \exists \eta_{1}, \mathbf{T} = \emptyset, \\ \mathbf{X}' = \mathbf{X} \cup \eta_{1} \cup (\operatorname{res}_{1} + 2 \mapsto -), \\ \chi \subseteq \chi' \}$ $(\operatorname{res}_{2}, -) \leftarrow \operatorname{getAndInc}() || e_{2};$

```
{∃ η<sub>1</sub>,η<sub>2</sub>, ι, \mathbf{T} = \emptyset,

\mathbf{X}^{\prime\prime} = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\operatorname{res}_1 + 2 \mapsto -) \cup (\operatorname{res}_2 + 2 \mapsto -),

\tau' \subseteq \tau'' \cup \operatorname{spent}(\chi'' \setminus \chi'),

\operatorname{last}(\mathbf{X}^{\prime\prime} \cup \chi') < \operatorname{res}_2 + 2 + 2 | \iota \cap \tau' |
```

```
return (res1, res2);
```

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res}_1 + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{\exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}^{\prime\prime} = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $T' \subseteq T'' \cup \text{spent}(\chi' \setminus \chi'),$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2 + 2 | \iota \cap \tau' |$

return (res1, res2);

$$\{ \mathbf{T} = \emptyset \}$$

 $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{\exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}^{\prime\prime} = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $T' \subseteq T'' \cup \text{spent}(\chi' \setminus \chi'),$

 $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2 + 2 | \iota \cap \tau'| \}$

```
return (res_1, res_2);
```

$$\{ \mathbf{T} = \emptyset \}$$

$$(\operatorname{res}_{1}, -) \leftarrow \operatorname{getAndInc}() \mid \mid e_{1};$$

$$\{ \exists \eta_{1}, \mathbf{T} = \emptyset, \\ \mathbf{X}' = \mathbf{X} \cup \eta_{1} \cup (\operatorname{res}_{1} + 2 \mapsto -), \\ \chi \subseteq \chi' \}$$

$$(\operatorname{res}_{2}, -) \leftarrow \operatorname{getAndInc}() \mid \mid e_{2};$$

$$\{ \exists \eta_{1}, \eta_{2}, l, \quad \mathbf{T} = \emptyset, \\ \mathbf{X}'' = \mathbf{X} \cup \eta_{1} \cup \eta_{2} \cup (\operatorname{res}_{1} + 2 \mapsto -) \cup (\operatorname{res}_{2} + 2 \mapsto -), \\ \mathbf{T}' \subseteq \mathbf{T}'' \cup \operatorname{spent}(\mathbf{X}'' \setminus \mathbf{X}'), \\ \operatorname{last}(\mathbf{X}'' \cup \chi') < \operatorname{res}_{2} + 2 + 2 \mid ln \mid \mathbf{T}' \mid \}$$

$$\operatorname{return} (\operatorname{res}_{1}, \operatorname{res}_{2}); \qquad \text{No more forked threads}$$

at this point!

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $\chi \subseteq \chi'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{\exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}^{\prime\prime} = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $\tau' \subseteq \emptyset \cup \operatorname{spent}(\emptyset)$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2 + 2 | \iota \cap \tau' |$ return (res1, res2);

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{\exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}'' = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $\tau' = \emptyset$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2 + 2 | \iota \cap \tau' |$ return (res1, res2);

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{\exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}'' = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $\tau' = \emptyset$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2 + 2 | \iota \cap \tau' |$ return (res1, res2);

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{ \exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}'' = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $\tau' = \emptyset$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2 + 2 | \iota \cap \emptyset |$ return (res1, res2);

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{\exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}'' = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $T' = \emptyset,$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2 + 2 \mid \emptyset \mid$ return (res1, res2);

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{ \exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}'' = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $T' = \emptyset,$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2$ return (res1, res2);

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res_1} + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{ \exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}^{\prime\prime} = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $T' = \emptyset,$ $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2$ return (res1, res2);

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res}_1 + 2 \mapsto -),$ $X \subseteq X'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{ \exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}^{\prime\prime} = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $T' = \emptyset$, $last(\mathbf{x}'' \cup \mathbf{x}') < res_2 + 2$ return (res1, res2);

$$\{ \mathbf{T} = \emptyset \}$$

$$(\operatorname{res}_{1}, -) \leftarrow \operatorname{getAndInc}() \mid \mid e_{1};$$

$$\{ \exists \eta_{1}, \mathbf{T} = \emptyset, \\ \mathbf{X}' = \mathbf{X} \cup \eta_{1} \cup (\operatorname{res}_{1} + 2 \mapsto -), \\ \chi \subseteq \chi' \}$$

$$(\operatorname{res}_{2}, -) \leftarrow \operatorname{getAndInc}() \mid \mid e_{2};$$

$$\{ \exists \eta_{1}, \eta_{2}, \mathsf{I}, \ \mathbf{T} = \emptyset, \\ \mathbf{X}'' = \mathbf{X} \cup \eta_{1} \cup \eta_{2} \cup (\operatorname{res}_{1} + 2 \mapsto -) \cup (\operatorname{res}_{2} + 2 \mapsto -), \\ \mathsf{T}' = \emptyset, \\ \operatorname{res}_{1} + 2 < \operatorname{res}_{2} + 2 \}$$

$$\operatorname{return} (\operatorname{res}_{1}, \operatorname{res}_{2});$$

 $\{ \mathbf{T} = \emptyset \}$ $(res_1, -) \leftarrow getAndInc() || e_1;$ $\{ \exists \eta_1, \mathbf{T} = \emptyset, \}$ $\mathbf{X}' = \mathbf{X} \cup \eta_1 \cup (\mathbf{res}_1 + 2 \mapsto -),$ $\chi \subseteq \chi'$ $(res_2, -) \leftarrow getAndInc() | | e_2;$ $\{ \exists \eta_1, \eta_2, \iota, \mathbf{T} = \emptyset, \}$ $\mathbf{X}'' = \mathbf{X} \cup \eta_1 \cup \eta_2 \cup (\mathbf{res_1} + 2 \mapsto -) \cup (\mathbf{res_2} + 2 \mapsto -),$ $T' = \emptyset$, $res_1 < res_2$ return (res1, res2);

Implications of the spec for getAndInc

- **R**₁: different calls return *distinct* results (strong concurrent counter)
- R₂: two calls, separated by *period of quiescence*, take effect in their sequential order (QC)
- R₃: results of *two calls* in the same thread are out of order by no more than 2 * (number of calls *interfering with both*) (QQC)

Summary of the proof pattern

- Express interference that matters via auxiliary state *tokens*;
- Capture past interference and results in auxiliary *histories*;
- Assume closed world to *bound* interference (quiescence).

What's in the paper

- Full formal specification of the counting network;
- Formal proofs of **QC** and **QQC** properties for the network;
- Discussion on applying the technique for *QC-queues*;
- Spec and verification of java.util.concurrent.Exchanger;
- Verification of an exchanger client in the spirit of concurrency-aware linearizability (CAL).
- Report on implementation in FCSL/Coq.



To take away

Hoare-style Specifications for Non-linearizable Concurrent Objects

- *Compositional* substitution principle;
- *Syntactic proof method* inference rules;
- Uniform reasoning about objects and their clients in the same proof system.

Good specification is in the eye of the beholder.

